# Analysis and Design of a 45° Slant-Polarized Omnidirectional Antenna

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Abstract-A 45° slant-polarized omnidirectional antenna is proposed for mobile communication base stations. The proposed antenna consists of four printed crossed-dipole elements which are rolled up into a cylinder for omnidirectional radiation. Each crossed-dipole element is composed of a horizontal dipole and a vertical dipole. The 45° slant polarization is achieved by adjusting the lengths of the horizontal and vertical dipoles. A broadband feeding network consisting of four broadband baluns and an impedance matching circuit is introduced to feed the four crossed-dipole elements. Experimental results show that the omnidirectionality or gain variation in the horizontal plane is less than 1 dB while the cross-polarization level is below -15 dB over a bandwidth of 15% (1.9-2.2 GHz). The 45° slant-polarized omnidirectional antenna has a bandwidth of 22% (1.75-2.18 GHz) for 15-dB return loss. Theoretical analysis and design procedure are presented.

*Index Terms*—45° slant polarization, base station antenna, mobile communications, omnidirectional antenna.

## I. INTRODUCTION

**I** N a mobile communication system, base station antennas with  $\pm 45^{\circ}$  slant polarization are commonly used because this type of polarization scheme offers more symmetrical propagation characteristics than vertical/horizontal polarization does [1]. A number of antennas have been proposed for  $45^{\circ}$  slantpolarized antenna [2]–[5]. However, all of these  $45^{\circ}$  slant-polarized antennas have a unidirectional radiation pattern which covers a sector (e.g.,  $120^{\circ}$ ) of azimuthal plane in a cellular system. For  $360^{\circ}$  coverage, antennas with an omnidirectional radiation pattern are required. It is well known that a vertically polarized omnidirectional antenna can be realized by a vertical dipole [6], while a horizontally polarized omnidirectional antenna may be obtained by a horizontal loop [7], [8]. A vertical/horizontal dual-polarized omnidirectional slot antenna was proposed in [9], but it is not  $45^{\circ}$  slant-polarized. For a

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 $45^{\circ}$  slant-polarized omnidirectional antenna, it is necessary to have an omnidirectional radiation pattern with equal horizontal and vertical components, including the same magnitude and the same phase. To the best of our knowledge, there are very few publications reporting  $45^{\circ}$  slant-polarized omnidirectional antennas. In [10], a bifilar helix antenna was claimed to be a  $45^{\circ}$ slant-polarized omnidirectional antenna. Unfortunately, it has been verified that this antenna is actually a circularly polarized omnidirectional antenna [11].

In this paper, a real  $45^{\circ}$  slant-polarized omnidirectional antenna is proposed. This antenna consists of four crossed-dipole elements which are wrapped around a cylinder for an omnidirectional radiation pattern. Each crossed-dipole element includes a horizontal dipole and a vertical dipole. The  $45^{\circ}$  slant polarization is realized by adjusting the lengths of the horizontal and vertical dipoles. A feeding network composed of four broadband baluns and an impedance matching circuit is designed to excite the  $45^{\circ}$  slant-polarized omnidirectional antenna, achieving a bandwidth of 22% (1.75–2.18 GHz) for 15-dB return loss. The cross-polarization level is below -15 dB and gain variation (or omnidirectionality [12]) is less than 1 dB (peak-to-peak) in the horizontal plane over a bandwidth of 15% (1.9–2.2 GHz).

Section II describes the configuration of the 45° slant-polarized omnidirectional antenna. Analysis and design are presented in Section III. An experimental verification is demonstrated in Section IV.

#### II. ANTENNA CONFIGURATION

The configuration of a 45° slant-polarized omnidirectional antenna is depicted in Fig. 1. The antenna includes four crossed-dipole elements and a feeding network. The four crossed-dipole elements are first printed on a thin flexible dielectric substrate and then rolled up into a hollow cylinder of diameter D (see Fig. 1(a)) to achieve an omnidirectional radiation pattern. Each crossed-dipole element is composed of a horizontal dipole and a vertical dipole (see Fig. 1(b)), which have lengths  $L_h$  and  $L_v$ , respectively. The 45° slant polarization is achieved by adjusting the lengths  $L_h$  and  $L_v$ . (Note that four 45° slanted dipoles cannot radiate an omnidirectional pattern with 45° slant polarization; instead they may generate a circularly polarized omnidirectional pattern [13], [14].) Four crossed-dipole elements are excited through a feeding network that comprises four broadband baluns and an impedance matching circuit (see Fig. 1(c)). A 50- $\Omega$  coaxial line is connected to the feeding network at the "Feeding point".

The  $45^{\circ}$  slant-polarized omnidirectional antenna was designed for UMTS (1.92–2.17 GHz) base stations at a center frequency of 2.05 GHz. The design procedure will be described

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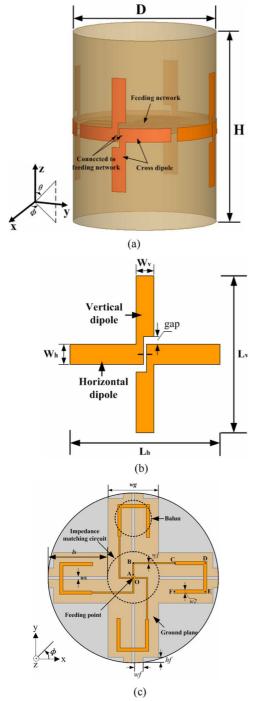


Fig. 1. Configuration of a 45° slant-polarized omnidirectional antenna: (a) Perspective view; (b) Crossed-dipole element; (c) Feeding network.

in the next section. The  $45^{\circ}$  slant-polarized omnidirectional antenna was simulated using Ansoft HFSS v13. The geometric parameters of the simulated antenna are listed in Table I.

#### III. ANALYSIS AND DESIGN

To understand the operating mechanism of the  $45^{\circ}$  slant-polarized omnidirectional antenna, we first define  $\pm 45^{\circ}$  slant-polarized electric field components as follows [15]:

$$E_{+45^\circ} = E_\phi \cos 45^\circ - E_\theta \sin 45^\circ \tag{1}$$

$$E_{-45^\circ} = E_\phi \cos 45^\circ + E_\theta \sin 45^\circ \tag{2}$$

 TABLE I

 GEOMETRIC PARAMETERS FOR THE 45° SLANT-POLARIZED ANTENNA

| Parameter                 | Value (mm) | Parameter      | Value (mm) |
|---------------------------|------------|----------------|------------|
| D                         | 77.6       | CD             | 13.7       |
| Н                         | 100.0      | DE             | 13.0       |
| $L_{h}$                   | 59.0       | EF             | 14.3       |
| $\mathbf{W}_{\mathrm{h}}$ | 8.0        | $\mathbf{W}_1$ | 0.6        |
| $L_v$                     | 64.0       | $W_2$          | 1.5        |
| $W_{v}$                   | 7.0        | ls             | 27.0       |
| gap                       | 3.0        | WS             | 1.2        |
| Wg                        | 23.0       | $h_{f}$        | 2.5        |
| OŠ                        | 6.7        | Wf             | 4.5        |
| BC                        | 19.0       | -              |            |

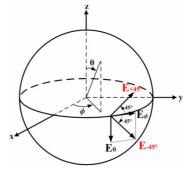


Fig. 2. Definition of 45° slant-polarized components.

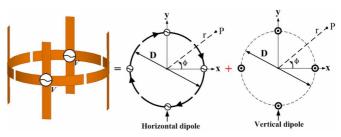


Fig. 3. Four crossed-dipole elements decomposed into four horizontal arc dipoles plus four vertical dipoles.

where  $E_{\theta}$  and  $E_{\phi}$  are the  $\theta$  and  $\phi$  components of the far-zone electric field, respectively, as illustrated in Fig. 2. Obviously, it is required for a purely 45° slant polarization to meet two conditions: 1) the magnitudes of  $E_{\theta}$  and  $E_{\phi}$  need to be equal, i.e.,  $|E_{\theta}| = |E_{\phi}|$ ; 2) the phases of  $E_{\theta}$  and  $E_{\phi}$  can be equal, i.e.,  $\angle E_{\theta} = \angle E_{\phi}$ , or have a 180° phase difference, i.e.,  $\angle E_{\theta} - \angle E_{\phi} = 180^{\circ}$ . For +45° slant polarization,  $|E_{\theta}| = |E_{\phi}|$  and  $\angle E_{\theta} - \angle E_{\phi} = 180^{\circ}$ , while for -45° slant polarization,  $|E_{\theta}| = |E_{\phi}|$  and  $\angle E_{\theta} | = |E_{\phi}|$  and  $\angle E_{\theta} = \angle E_{\phi}$ .

Four rolled crossed-dipole elements can be decomposed into four horizontal arc dipoles plus four vertical straight dipoles, as shown in Fig. 3. To simplify the analytical procedure, we replace the four horizontal arc dipoles with four straight dipoles, as illustrated in Fig. 4.

It is assumed that the current distribution on every dipole is sinusoidal. The far-zone electric field radiated by four vertical dipoles in the horizontal plane (i.e.,  $\theta = 90^{\circ}$ ) is (see Appendix)

$$E_{\theta} = j \frac{120I_v e^{-jkr}}{r} \left( 1 - \cos\left(\frac{kL_v}{2}\right) \right) \left[ \cos\left(\frac{kD}{2}\cos\phi\right) + \cos\left(\frac{kD}{2}\sin\phi\right) \right]$$
(3)

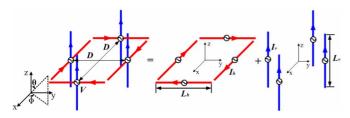


Fig. 4. Simplified crossed-dipole elements and associated decomposition.

where  $I_v$  is the amplitude of the sinusoidal current on the vertical dipoles and  $k = 2\pi/\lambda$  is the wave number with  $\lambda =$  wavelength in free space at the center frequency of an operating frequency band.

Similarly, the electric field radiated by four horizontal dipoles in the horizontal plane (i.e.,  $\theta = 90^{\circ}$ ) can be found to be (also see Appendix)

$$E_{\phi} = -\frac{120I_{h}e^{-jkr}}{r} \left\{ \frac{\sin\left(\frac{kD}{2}\sin\phi\right)}{\sin\phi} \times \left(\cos\left(\frac{kL_{h}}{2}\cos\phi\right) - \cos\left(\frac{kL_{h}}{2}\right)\right) + \frac{\sin\left(\frac{kD}{2}\cos\phi\right)}{\cos\phi} \left(\cos\left(\frac{kL_{h}}{2}\sin\phi\right) - \cos\left(\frac{kL_{h}}{2}\right)\right) \right\}$$
(4)

where  $I_{\rm h}$  is the amplitude of the sinusoidal current on the horizontal dipoles.

There are three critical parameters for the 45° slant-polarized omnidirectional antenna, including the diameter of the hollow cylinder (D) and the lengths of the horizontal and vertical dipoles ( $L_h$  and  $L_v$ ), which are determined as follows.

#### A. Determination of Antenna Diameter (D)

According to the definition of  $45^{\circ}$  slant polarization, the first necessary condition is  $|E_{\theta}| = |E_{\phi}|$ , or  $|E_{\theta}|/|E_{\phi}| = 1$ . We calculate  $|E_{\theta}|/|E_{\phi}|$  using (3) and (4) for a dipole length of a half-wavelength (i.e.,  $L_v = L_h = \lambda/2$ ) and plot  $|E_{\theta}|/|E_{\phi}|$  as a function of the azimuthal angle  $\phi$  for difference values of the antenna diameter (D) in Fig. 5. It can be seen that when D =  $0.6\lambda$ ,  $|E_{\theta}|/|E_{\phi}|$  varies around 0.6 and the variation (peak-topeak) is larger than 0.3. When D =  $0.4\lambda$ , the variation is less than 0.1 but  $|E_{\theta}|/|E_{\phi}|$  is larger than 1.3. As D is close to a half-wave length,  $|E_{\theta}|/|E_{\phi}|$  is close to 1. The optimal value for the antenna diameter is D =  $0.475\lambda$  at which  $|E_{\theta}|/|E_{\phi}|$  varies around 1 and the variation is less than 0.2. Note that this optimal value is found for the simplified crossed-dipole elements with straight horizontal dipole.

For the original crossed-dipole elements with horizontal arc dipoles, the antenna diameter should be slightly larger than  $0.475\lambda$ . By simulation, the optimized antenna diameter is found to be close to a half-wave length, i.e.,  $D \cong 0.5\lambda$ .

### B. Determination of Lengths $(L_h \text{ and } L_v)$

Based on the definition of 45° slant polarization, the second necessary condition requires the phases of  $E_{\theta}$  and  $E_{\phi}$  to be

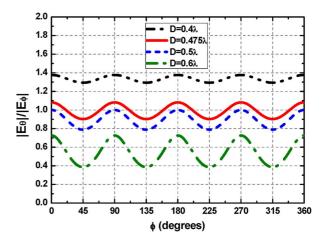


Fig. 5.  $|E_{\theta}|/|E_{\phi}|$  for different values of the antenna diameter (D).

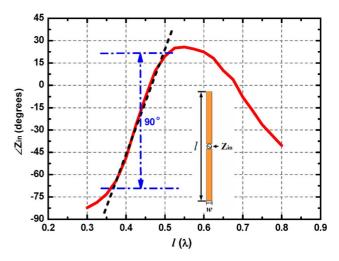


Fig. 6. The phase  $\angle Z_{in}$  of the input impedance  $Z_{in}$  for a printed dipole as a function of the dipole length *l*.

equal, i.e.,  $\angle E_{\theta} = \angle E_{\phi}$ , or to have a 180° difference, i.e.,  $\angle E_{\theta} - \angle E_{\phi} = 180^{\circ}$ . From (3) and (4), we can see that  $E_{\theta}$ and  $E_{\phi}$  would have a 90° phase difference if the current  $(I_h)$ on the horizontal dipoles is in phase with the current  $(I_v)$  on the vertical dipoles. The currents  $(I_h \text{ and } I_v)$  depend on the phase  $(\angle Z_{in})$  of the input impedance  $Z_{in}$  of each dipole, which varies with the length of the dipole. Fig. 6 shows the phase  $\angle Z_{in}$  simulated for a printed dipole with width  $w = 0.05\lambda$  as a function of the dipole length l. It is seen that a 90° phase difference can be obtained by changing the length l approximately from  $l = 0.35\lambda$  to  $l = 0.5\lambda$ . This means that the lengths of the horizontal and vertical dipoles  $(L_h \text{ and } L_v)$  can be chosen to be  $L_h = \sim 0.35\lambda$  and  $L_v = \sim 0.5\lambda$ .

Considering the mutual coupling and the actual current distributions on the crossed-dipole elements, we optimized the lengths  $L_h$  and  $L_v$  by simulation. Fig. 7 shows the magnitude ratio  $(|E_{\theta}|/|E_{\phi}|)$  and phase difference  $(\angle E_{\theta} - \angle E_{\phi})$  as a function of  $L_v$  for different values of  $L_h$ . From Figs. 7(a) and (c), it is seen that when  $L_h = 0.375\lambda$  and  $0.425\lambda$ , it is impossible to satisfy the conditions  $|E_{\theta}|/|E_{\phi}| = 1$  and  $\angle E_{\theta} - \angle E_{\phi} = 180^{\circ}$  for the same  $L_v$ . This implies that 45° slant polarization cannot be achieved for  $L_h = 0.375\lambda$  and  $0.425\lambda$ . From Fig. 7(b), it can be seen that when  $L_h = 0.4\lambda$  and  $L_v = 0.45\lambda$ , both the

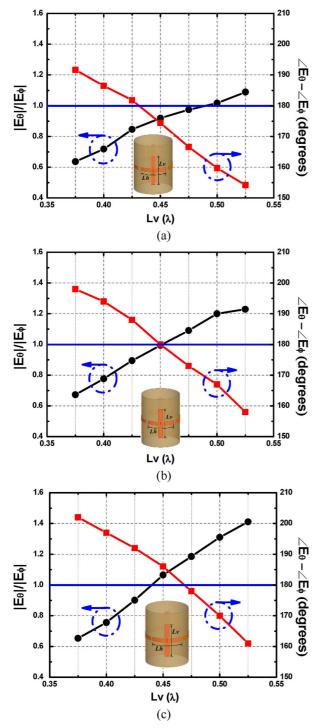


Fig. 7. Magnitude ratio  $(|E_{\theta}|/|E_{\phi}|)$  and phase difference  $(\angle E_{\theta} - \angle E_{\phi})$  as a function of  $L_v$  for different values of  $L_h$ : (a)  $L_h = 0.375\lambda$ ; (b)  $L_h = 0.4\lambda$ ; (c)  $L_h = 0.425\lambda$ .

conditions  $|E_{\theta}|/|E_{\phi}| = 1$  and  $\angle E_{\theta} - \angle E_{\phi} = 180^{\circ}$  are satisfied; thus +45° slant polarization can be achieved. For -45° slant polarization, it is easy to be obtained by switching the connecting points between the horizontal and vertical dipoles. Fig. 8 demonstrates the magnitude ratio  $(|E_{\theta}|/|E_{\phi}|)$  and phase difference  $(\angle E_{\theta} - \angle E_{\phi})$  as a function of frequency for the optimized lengths  $L_{h} = 0.4\lambda$  and  $L_{v} = 0.45\lambda$ . It is seen that  $|E_{\theta}|/|E_{\phi}| = 1 \pm 0.2$  and  $\angle E_{\theta} - \angle E_{\phi} = 180 \pm 4^{\circ}$  over the frequency range 1.9–2.2 GHz.

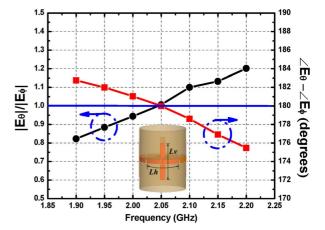


Fig. 8. Magnitude ratio  $(|E_{\theta}|/|E_{\phi}|)$  and phase difference  $(\angle E_{\theta} - \angle E_{\phi})$  as a function of frequency for  $L_h = 0.4\lambda$  and  $L_v = 0.45\lambda$ .

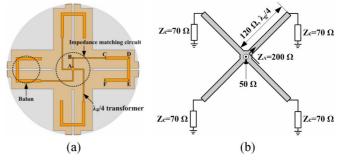


Fig. 9. Feeding network (a) and its equivalent circuit (b) for the 45° slantpolarized omnidirectional antenna.

## C. Feeding Network

A feeding network consisting of four broadband baluns and an impedance matching circuit is introduced to feed the four crossed-dipole elements. The input impedance of the broadband balun for each crossed-dipole element (e.g., looking at Point "C" in Fig. 9(a)) is designed to be 70  $\Omega$ . The theoretical analysis of the broadband balun can be found in [16]. To match four broadband baluns connected in parallel to a 50- $\Omega$  coaxial line, an impedance matching circuit is needed. An equivalent circuit for the impedance matching is depicted in Fig. 9(b). The broadband balun was simplified as a 70- $\Omega$  impedance The 70- $\Omega$  impedance looking at Point "C" ( $Z_C = 70 \ \Omega$ ) is transformed into a 200- $\Omega$ impedance at Point "A" ( $Z_A = 200 \ \Omega$ ) by a 120- $\Omega$  quarterwave  $(\lambda_{\rm g}/4)$  transformer  $(\sqrt{200 \ \Omega \times 70 \ \Omega} = 120 \ \Omega)$ . Then the four 200- $\Omega$  impedances are connected in parallel, resulting in a 50- $\Omega$  impedance, matching to the 50- $\Omega$  coaxial line at the center of the feeding network. The simulated input impedances from 1.7-2.2 GHz at different points of the feeding network are shown in Fig. 10. It can be seen that the input impedance for each crossed-dipole element  $(Z_{dipole})$  is capacitive. After impedance transformation through the slot-line coupling, the impedance ( $Z_c$ ) at Point "C" is approximately equal to 70  $\Omega$ at the center frequency 2.05 GHz. Following the quarter-wave transformer, the total input impedance (Z<sub>in</sub>) of the feeding network is matched to 50  $\Omega$ .

#### IV. EXPERIMENTAL VERIFICATION

To verify the design, the 45° slant-polarized omnidirectional antenna was fabricated and measured. Fig. 11 shows a picture

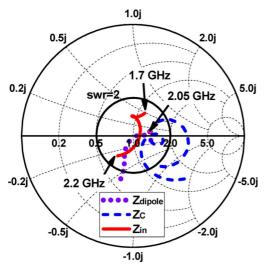


Fig. 10. Simulated input impedances at different points of the feeding network.



Fig. 11. A picture of the prototype of a  $45^{\circ}$  slant-polarized omnidirectional antenna with feeding network.

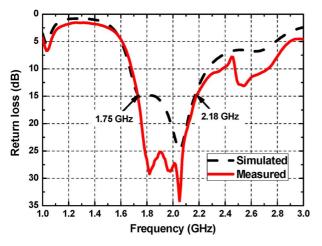


Fig. 12. Simulated and measured results for return loss of the  $45^{\circ}$  slant-polarized omnidirectional antenna.

of the antenna prototype with the front and back views of the feeding network. Four crossed-dipole elements were first printed on a Panasonic R-F775 flexible dielectric substrate ( $\varepsilon_r = 3.2$ , loss tangent = 0.0015, thickness = 0.05 mm)

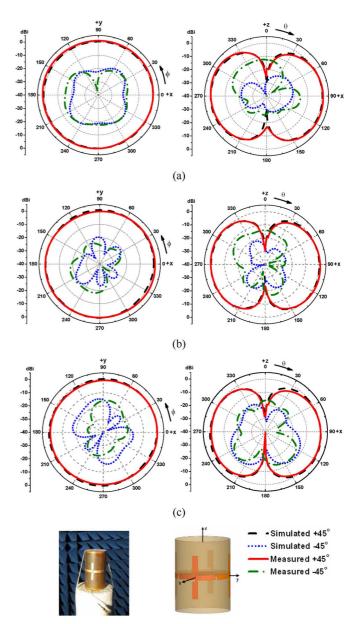


Fig. 13. Simulated and measured radiation patterns of the  $45^{\circ}$  slant-polarized omnidirectional antenna at (a) 1.9 GHz, (b) 2.05 GHz, and (c) 2.2 GHz.

and then rolled up into a hollow cylinder. The feeding network was printed on a Taconic TLY-5 dielectric substrate ( $\varepsilon_r = 2.2$ , loss tangent = 0.0009, thickness = 0.8 mm). A flexible coaxial line (Johnson/Emerson RG178) with an SMA connector is connected to the feeding network.

Fig. 12 shows simulated and measured results of return loss (RL). Good agreement is observed. The measured bandwidth for RL > 15 dB is about 22% (1.75 GHz–2.18 GHz). The radiation patterns of the 45° slant-polarized omnidirectional antenna simulated and measured at 1.9, 2.05, and 2.2 GHz are plotted in Fig. 13. The radiation pattern was measured using a SATIMO antenna measurement system SG24 at the Speed Communication Technology Corporation Ltd., Shenzhen, China. It is observed that the gain variation in the horizontal plane (i.e., the x-y plane) is less than 1 dB, confirming a good omnidirectionality. The cross-polarization level (i.e., the  $-45^{\circ}$  polarized component) is -15 dB below the co-polarization (i.e., the  $+45^{\circ}$  po

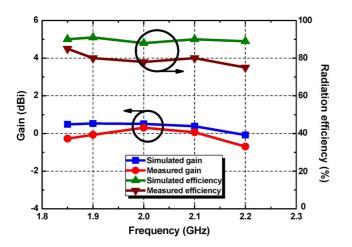


Fig. 14. Gain and radiation efficiency for the  $45^\circ$  slant-polarized omnidirectional antenna.

larized component) in the horizontal plane. Fig. 14 presents the simulated and measured gains of the 45° slant-polarized omnidirectional antenna. The measured gain is around 0 dBi, which is lower than the gain of a typical half-wave dipole antenna. The lower gain is mainly due to the broader beamwidth in the elevation plane, which is found to be  $\sim 120^{\circ}$  (half-power beamwidth), much wider than 78° for a half-wave dipole. The radiation efficiency of the 45° slant-polarized omnidirectional antenna is about 80% (also see Fig. 14). The simulated efficiency is slightly higher than measured result because the simulation did not take the feeding coaxial line into account.

## V. CONCLUSION

A  $45^{\circ}$  slant-polarized omnidirectional antenna is developed by utilizing four crossed-dipole elements. The operating mechanism and design method are elaborated. The  $45^{\circ}$  slant-polarized omnidirectional antenna achieves a bandwidth of 22% (1.75–2.18 GHz) for 15-dB return loss. The gain variation is less than 1 dB and the cross-polarization level is below -15dB over a bandwidth of 15% (1.9–2.2 GHz). This broadband omnidirectional antenna may find applications in base stations for mobile communications.

## APPENDIX

## DERIVATION OF $E_{\theta}$ IN (3) AND $E_{\phi}$ IN (4)

Consider a vertical dipole of length L placed coincidently with the z axis and with its center at the origin. Assume a sinusoidal current distribution on the dipole. The far-zone electric field for the vertical dipole in the horizontal plane (i.e.,  $\theta = 90^{\circ}$ ) is given by [6], [17]

$$E_{\theta} = j\eta \frac{I_0}{2\pi r} \left( 1 - \cos\left(\frac{kL}{2}\right) \right) e^{-jkr}$$
(A1)

where  $I_0$  is the amplitude of the sinusoidal current on the dipoles and  $\eta \cong 120\pi$  is the intrinsic impedance of the free space.

For four vertical dipoles equally spaced along a circular ring of radius R, as shown in Fig. A1, the far-zone electric field in the

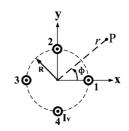


Fig. A1. Four vertical dipoles.

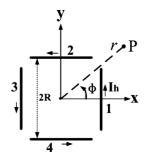


Fig. A2. Four horizontal dipoles

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horizontal plane for each dipole can be approximately expressed for  $r \gg R$  as

$$E_{\theta 1} = j\eta \frac{I_v e^{-jkr}}{2\pi r} \left(1 - \cos\left(\frac{kL}{2}\right)\right) e^{jkR\cos\phi}$$
(A2)

$$E_{\theta 2} = j\eta \frac{I_v e^{-jkr}}{2\pi r} \left(1 - \cos\left(\frac{kL}{2}\right)\right) e^{jkR\sin\phi}$$
(A3)

$$E_{\theta 3} = j\eta \frac{I_v e^{-jkr}}{2\pi r} \left(1 - \cos\left(\frac{kL}{2}\right)\right) e^{-jkR\cos\phi} \quad (A4)$$

$$E_{\theta 4} = j\eta \frac{I_v e^{-jkr}}{2\pi r} \left(1 - \cos\left(\frac{kL}{2}\right)\right) e^{-jkR\sin\phi} \quad (A5)$$

Thus, the total electric field is the sum of fields from the four vertical dipoles as given by (3).

For four horizontal dipoles placed along a square of side length 2R, as shown in Fig. A2, the far-zone electric field in the horizontal plane for each dipole can be found to be

$$E_{\phi 1} = -j\eta \frac{I_h e^{-jkr}}{2\pi r} \frac{1}{\cos\phi} \left( \cos\left(\frac{kL}{2}\sin\phi\right) - \cos\left(\frac{kL}{2}\right) \right) e^{jkR\cos\phi}$$
(A6)

$$E_{\phi 2} = -j\eta \frac{I_h e^{-jkr}}{2\pi r} \frac{1}{\sin\phi} \left( \cos\left(\frac{kL}{2}\cos\phi\right) - \cos\left(\frac{kL}{2}\right) \right) e^{jkR\sin\phi}$$
(A7)

$$E_{\phi 3} = j\eta \frac{I_h e^{-jkr}}{2\pi r} \frac{1}{\cos\phi} \left( \cos\left(\frac{kL}{2}\sin\phi\right) - \cos\left(\frac{kL}{2}\right) \right) e^{-jkR\cos\phi}$$
(A8)

$$E_{\phi 4} = j\eta \frac{I_h e^{-jkr}}{2\pi r} \frac{1}{\sin\phi} \left( \cos\left(\frac{kL}{2}\cos\phi\right) - \cos\left(\frac{kL}{2}\right) \right) e^{-jkR\sin\phi}$$
(A9)

Therefore, the sum of electric fields from the four horizontal dipoles leads to the total electric field given by (4).

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